7.3 Multiply and Divide Rational Expressions

Simplify the following rational expressions.

a.
$$\frac{14x^5 - 22x^3 + 9x}{2x^2}$$

b.
$$\frac{40x^3}{6y} \cdot \frac{15y^2}{5x^5}$$

c.
$$\frac{a+5}{a-2} \cdot \frac{a-3}{a+4}$$

Multiply the following rational expressions.

a.
$$\frac{(h+2)(h-8)}{(h-6)(h+3)}$$

$$(h-8)(h-6)$$
 $(h-2)(h-7)$

Divide the following rational expressions. b. $\frac{8}{15} \div \frac{4}{7}$ c. $\frac{d+3}{d-5} \div \frac{d+3}{d+8}$

Divide the following rational expressions.

c.
$$\frac{18x^2 + 9x - 20}{x^2 + 2x - 35} \div \frac{6x^2 + 13x - 15}{x^2 + 10x + 21}$$

7.4 Add and Subtract Rational Expressions

Find the least common denominator for each of the following sets of fractions and rewrite each fraction in terms of the LCD.

a.
$$\frac{5}{6x^2}$$
 $\frac{4}{5x^5}$ b. $\frac{a+2}{a-5}$ $\frac{a-3}{a+7}$

Find the least common denominator for each of the following sets of fractions and rewrite each fraction in terms of the LCD.

a.
$$\frac{2x+5}{x^2+10x+25}$$
 $\frac{3x-4}{x^2+2x-15}$

Add the following rational expressions.

a.
$$\frac{8}{3a^2} + \frac{2}{7a}$$
 b. $\frac{h+6}{h+2} + \frac{h-5}{h+2}$

Add the following rational expressions.

c.
$$p + \frac{3}{p-5}$$

Add the following rational expressions.

d.
$$\frac{a+2}{a^2+5a-6} + \frac{a-3}{a^2+8a+12}$$

Subtract the following rational expressions.

a.
$$\frac{x^2 + 5x}{(x+3)(x+4)} - \frac{3x+8}{(x+3)(x+4)}$$
 b. $\frac{5x+2}{x^2 - 7x + 12} - \frac{2x-7}{x^2 + 4x - 21}$

7.5 Solving Rational Equations

Steps:

- 1. State what values should be excluded
- 2. Multiply both sides of the equation by the Least Common Denominator (LCD) or cross multiply if possible
- 3. Solve the remaining equation
- 4. Check the answer(s) in the original equation.(Watch for division by zero).

Solve the following rational equation. Check your answer in the original equation.

a.
$$\frac{35}{x+3} = 5$$

b.
$$\frac{8}{x+3} = 7 - \frac{6}{x+3}$$

Solve the following rational equations. Check your answer in the original equation.

c.
$$\frac{3}{a+2} + \frac{5a}{a-3} = \frac{75}{a^2 - a - 6}$$