## Intermediate Algebra

## Chapters 6 \& 7 Practice Test, Calculator Allowed

I. Sketch the graph of the following. Show any vertical asymptotes as dashed lines. Also, identify the domain.

1. $f(x)=\frac{3.2}{x^{2}-1}$
2. $f(x)=\frac{-1}{x-1}$
3. $f(x)=\frac{-3}{(x-4)^{2}}$
II. Evaluate $f(x)$ at the given value of $x$.
4. $\quad f(x)=\frac{3.2}{x^{2}-1}$ for $x=-1.4$
5. $f(x)=\frac{3 x^{2}+2 x}{7 x}$ for $x=-3$
6. $\quad f(x)=\frac{6 x^{2}-4 x+5}{9-x}$ for $x=9$
III. Simplify the following problems by performing the indicated operations. Write all fractions in lowest terms.
7. $\frac{x^{2}+3 x+2}{2 x^{2}-x-10}$
8. $\frac{x^{2}+4}{x^{2}-4} \cdot \frac{x+2}{x-2}$
9. $\frac{1}{8 x^{2}} \div \frac{1}{2 x^{3}}$
10. $\frac{2 x-6}{6 x^{2}-15 x} \div \frac{4 x-12}{18 x^{2}-45 x}$
IV. Solve.
11. $\frac{x+1}{5}=\frac{x}{3}$
12. $\frac{3}{7}=\frac{4}{x-1}$
V. Solve the problem.
13. In the following formula, y is the minimum number of hours of studying required to attain a test score of $\mathrm{x}: ~ y=\frac{0.32 x}{100.5-x}$. How many hours of studying are needed to score 86 ? Round to the nearest hundredth of an hour.
14. The area A of a rectangle is $5 x^{2}+13 x-6$ and its width W is $x+3$. Find the length L of the rectangle.
15. If 3.2 ounces of oil are to be added to 16 gallons of gasoline, then $x$ ounces of oil should be added to 37 gallons of gasoline.
a) Write the proportion.
b) Solve for x .
IV. Simplify the following problems by performing the indicated operations. Write all radical answers in simplified form, NOT as decimals.
16. $\left(2 x^{-3} y^{1 / 3}\right)^{3}$
17. $\left(\frac{1}{2} x^{2} y^{-3}\right)^{3}$
18. $\sqrt{3 x^{3}} \cdot \sqrt{27 x^{3}}$
19. $\sqrt{18} \cdot \sqrt{2}$
20. $4 \sqrt[3]{16}-5 \sqrt[3]{2}$
21. $\sqrt{5}+3 \sqrt{2}-7 \sqrt{5}$
22. $\frac{\sqrt{45 x^{3} y^{3}}}{\sqrt{5 y}}$
23. $\frac{\sqrt{98 x^{2} y^{3}}}{\sqrt{x y}}$
24. $\frac{\sqrt[3]{27 y^{7}}}{\sqrt[3]{x^{6} y^{2}}}$
25. $\frac{\sqrt[3]{32 x^{4}}}{\sqrt[3]{-4 y^{3}}}$
V. Simplify the following complex expressions by performing the indicated operations. Write all answers in standard form.
26. $(7-4 i)(-2-i)$
27. $(2+3 i)(3-5 i)$
28. $(7-i \sqrt{5})^{2}$
29. $(6+i)(6-i)$
30. $\frac{3+4 i}{2 i}$
31. $\frac{2+3 i}{4-2 i}$
VI. Find the domain of $f$, write your answer in interval notation.
32. $f(x)=\sqrt{4-6 x}$
33. $f(x)=\sqrt{2 x^{2}+3}$

## Answers:

I. Use a calculator to sketch your graphs!

1. Vertical Asymptote: $x= \pm 1$, Domain: All reals excluding $x= \pm 1$
2. Vertical Asymptote: $x=1$, Domain: All reals excluding $x=1$
3. Vertical Asymptote: $x=4$, Domain: All reals excluding $x=4$
4. $f(-1.4)=\frac{10}{3}$
5. $f(-3)=-1$
6. undefined
7. $\frac{x+1}{2 x-5}$
8. $\frac{x^{2}+4}{(x-2)^{2}}$
9. $\frac{x}{4}$
10. $\frac{3}{2}$
11. $x=\frac{3}{2}$
12. $x=\frac{31}{3}$
13. 1.9 hours
14. $5 x-2$
15. a) $\frac{3.2}{16}=\frac{x}{37}$
b) 7.4 ounces
16. $\frac{8 y}{x^{9}}$
17. $\frac{x^{6}}{8 y^{9}}$
18. $9 x^{3}$
19. 6
20. $\quad 3 \sqrt[3]{2}$
21. $3 \sqrt{2}-6 \sqrt{5}$
22. $3 x y \sqrt{x}$
23. $\frac{3 y \sqrt[3]{y^{2}}}{x^{2}}$
24. $-18+i$
25. $7 y \sqrt{2 x}$
26. $44-14 i \sqrt{5}$
27. $\frac{-2 x \sqrt[3]{x}}{y}$
28. $\frac{-4+3 i}{-2}$
29. $\left(-\infty, \frac{2}{3}\right]$
30. $21-i$
31. 37
32. $\frac{1+8 i}{10}$
33. $(-\infty, \infty)$
