# TR 10am

#### **Solving Quadratic Equations by Factoring**

#### **Names of Group Members:**

Zero-Product Property: If ab = 0, then either a = 0 or b = 0, or both. (When two or more numbers are multiplied together and the result is zero, then one of them must equal zero.

## Steps to Solve:

- 1. The equation must be in standard form  $(ax^2 + bx + c = 0)$  and equal to zero. If it is not equal to zero, then you cannot use the zero-product property.
- 2. Factor the trinomial into 2 binomials.
- 3. Set each binomial equal to zero and solve for the variable.
- 4. You can verify these solutions in the original equation.

#### Examples:

1. 
$$x^{2} + 3x - 10 = 0$$
  $x + 5 = 0$   $x - 2 = 0$   $x - 2 = 0$   $x - 5$   $x = 2$   $x - 3$   $x - 2$   $x = 3$   $x - 2$   $x = 3$   $x - 3$ 

4. The height above ground of a ball thrown at 64 feet per second from the top of an 80-foot-high building is modeled by  $S = 80 + 64t - 16t^2$  feet, where t is the number of seconds after the ball is thrown. How long will the ball be in the air?

$$-1/6(t^2+1.64t+80=0)$$
  
 $-1/6(t^2-4t-5)=0$  The ball will  
 $-1/6(t-5)(t-1)$  be in the air  
 $-1/6(t-5)(t-1)$  for 5 seconds.  
 $t-5=0$   $t+1=0$  for 5 seconds.

## Solving Quadratic Equations by Graphical & Numerical Methods

#### **Names of Group Members:**

Graphical: where the graph intercepts the x-axis is the solution(s) to the quadratic equation.

#### Steps to Solve:

- 1. The equation must be in standard form  $(ax^2 + bx + c = y)$ .
- 2. Set  $y_1$  = the equation, then graph.
- 3. Use 2<sup>nd</sup> Trace option 2:zero, identify left bound, right bound, and guess for calculator to identify zero.
- 4. You can verify these solutions in the original equation.

## Examples:

1. 
$$2x^2 + x - 6 = 0$$
  
 $X = 1.5$  and  $X = -2$ 

2. 
$$6x^2 + 5x - 6 = 0$$

3. 
$$10x^{2} = 22x - 4$$

$$10x^{2} - 20x + 4$$

$$X = 2000 \quad X = 2$$

4. 
$$x^2 + 4x = -8$$
  
 $x^2 + 4x + 8 = 0$   
NO Solution

## **Solving Quadratic Equations by Graphical & Numerical Methods**

#### **Names of Group Members:**

Numerical: in a table when the  $y_1 = 0$ , the corresponding x-value(s) are the solution(s).

## Steps to Solve:

- 1. The equation must be in standard form  $(ax^2 + bx + c = y)$ .
- 2. Set  $y_1$  = the equation, then use  $2^{nd}$  Graph to create a table. Adjust the table setup as needed using  $2^{nd}$  Window.
- 3. Locate the  $y_1 = 0$ , then select the corresponding x-values.
- 4. You can verify these solutions in the original equation.

## Examples:

3.  $2x^2 + 7x = 4$ 

1. 
$$x^2 - 7x + 10 = 0$$
  
 $X = 2$  and  $X = 5$ 

2. 
$$x^2 - 9x + 18 = 0$$
  
 $X = 3$  and  $X = 6$ 

$$X = .5$$
 and  $X = -4$ 

## **Solving Quadratic Equations by Square Root Method**

## **Names of Group Members:**

Square Root Property: If  $x^2 = a$ , then  $x = \sqrt{a}$  or  $x = -\sqrt{a}$ , so the solutions of the quadratic equation of the form  $x^2 = a$  are given by  $x = \pm \sqrt{a}$ .

## Steps to Solve:

- 1. The equation must not have a bx term.
- 2. Isolate the squared term.
- 3. Apply the square root property, by taking the square root of both sides.
- 4. If there is a variable expression, then solve for the variable.
- 5. You can verify these solutions in the original equation.

## Examples:

1. 
$$x^2 = 20$$
  $x = 20$   $x = 20$   $x = 20$ 

2. 
$$5x^2 - 25 = 0$$

$$5x^{2} = 25 = 5 = 5 \times 2 = 25 \times 2 = 25$$

4. 
$$(2x+1)^2 + 7 = 0$$

$$-7 - 7$$

$$(2x+1)^2 = -7 / (2x+1)^2 = \pm i\sqrt{7} / (2$$

## Solving Quadratic Equations by Completing the Square

#### Names of Group Members:

Completing the Square: when you can't factor the trinomial then your split up the trinomial and can use a version of the square root method.

#### Steps to Solve:

- 1. The equation must have the variables on one side of the equal sign and the constant on the other side  $(x^2 + bx = d)$ .
- 2. First you must determine what the "c" value should be in order to create a perfect square trinomial:  $c=\left(\frac{b}{2}\right)^2$ .
- 3. Then add  $\left(\frac{b}{2}\right)^2$  to both sides.
- 4. Rewrite the perfect square trinomial in the form of a binomial squared  $\left(x + \frac{b}{2}\right)^2$  and simplify the constants on the right hand side.
- 5. Now use the square root method to solve for x.
- 6. You can verify these solutions in the original equation.

#### Examples:

1. 
$$x^{2} + 4x - 9 = 0$$
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## **Solving Quadratic Equations by Quadratic Formula**

#### **Names of Group Members:**

Quadratic Formula: solutions of the quadratic equation of the form  $ax^2 + bc + c = 0$  are given by  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ .

## Steps to Solve:

- 1. The equation must be in standard form  $(ax^2 + bx + c = 0)$ .
- 2. Replace each letter with its appropriate coefficients from the quadratic equation.
- 3. Simplify the formula.

