## Graphing Calculator Basics <br> TI-83, TI-83 ${ }^{+}$, TI-84 and TI-84 ${ }^{+}$

Note: This is a brief handout on basic graphing calculator functions. Click "Graphing Calculator Help" on your BB course page for tutorials on the features of the graphing calculator. You will need to use the graphing calculator throughout this course. It is important that you also review the referred tutorials so that you learn more about using this important tool.

## I. Basic functions

## Display:

To darken or lighten screen, use $2 n d$ or $\square$ arrows.

## Erasing:

Delete $\rightarrow$ Use DEL to erase last entry
Clear $\rightarrow$ Use CLEAR to erase all entries

## The two minuses:

Use ( --1 (to the left of ENTER) for negative umbers
Use $\square$ (right above the $\square$ key) for minus or subtraction

## Exponents:

Use the $\triangle$ (upper caret) symbol
Ex. $3^{4} \rightarrow 3 \boxed{ } 4$
The square key is give by default:
Ex. $3^{2} \rightarrow 3 x^{2}$

## Roots:

Square root: $[\checkmark]$ will take the square root of a nonnegative number or expression.

$$
\text { Ex. } \sqrt{16} \rightarrow \text { 2nd } \sqrt{( } 16) \text { ENTER }
$$

Note: If the expression is negative you will get an error message
Other roots: The easiest way is to use the $(1 / n)$ definition
Ex. Cube root of $8 \rightarrow 8$ (1/3)
[Note: Use the division key $\square$ to type the fraction bar]
Fifth root of $1024 \rightarrow 1024 \triangle(1 / 5)$

## Changing screens:

2nd [QuIT] takes you back to the home screen.
( [QUIT] is found above MODE )

## Mode:

Use FLOAT to change the number of decimal places. Be sure to check your instructor's request on your tests; you may be asked to find the answer with 0 decimal places, or 2,3 , or 4 , etc. To change it, just place the cursor on the desired number of decimal places and press ENTER.

(The TI-83 does not show the "Set Clock" option)

## II. Graphing

Viewing Window key: WINDOW
Tells us the portion of the coordinate system we are viewing when we look at our graph; change your window to see more or less of your graph.

Standard window (Zoom 6): From -10 to 10 on both axes.


## Graphing Lines:

Ex. Graph $y-5=2 x$.

First, ' ${ }^{\prime}$ " ' must be isolated, so $y=2 x+5$.

Go to $Y=$ and type in the equation, then press GRAPH
Note: Use $X, T, \Theta, \eta$ to type the " $x$ " variable

| $\begin{aligned} & \text { F1ot1 F1otz Fots } \\ & Y_{1}=2 \times+5 \\ & y_{2}= \\ & y_{3}= \\ & \forall y_{5}= \\ & y_{6}= \\ & y_{7}= \end{aligned}$ |
| :---: |

(
[Important! : If you see any "Plot" highlighted, move the cursor up to it and press ENTER to deactivate it; no "Plot" should be activated.]

Correct

| Floti | Flote plots |
| :---: | :---: |
| $V_{2}=$ |  |
| Vz= |  |
| $\mathrm{V}_{4}=$ |  |
| $V_{5}=$ |  |
| $V_{6}=$ |  |

Incorrect

|  | Flote Flots |
| :---: | :---: |
| $\sqrt{y_{1}}=$ |  |
| $v_{3}=$ |  |
| $\cdots 4=$ |  |
| Y5= |  |
| V6= |  |
| $\cdots 7=$ |  |

Ex. $y=\frac{1}{2} x-6$
When entering fractions, always enclose them within parentheses!
Go to $Y$ and enter $\mathrm{y}=\square 1 / 2 \square \mathrm{x}-6$ then choose GRAPH
[Note: Use the division key to type the fraction bar]


Notice that we cannot see the $x$-intercept! An appropriate window for a line should always show both $x$-and- $\boldsymbol{y}$ intercepts. The point where this line crosses the $x$-axis is beyond our standard viewing window (which gives us a maximum value of 10 for the X -axis).

Therefore, we must assign a larger value to Xmax.
Press the WINDOW key and change Xmax to 15 , or any larger value, until you clearly see the $x$-intercept.
Example:


Appropriate window!

## Quadratics:

Ex. $y=2 x^{2}-15$
Go to $Y \exists$ and enter the equation, then choose GRAPH


This is another case where the window must be expanded to accommodate the vertex of this curve (parabola). The Ymin value of -20 would give us a more appropriate viewing window:


## Special Functions:

Ex. Absolute value function $y=|x|+2$
Go to $Y$ and enter the equation into the calculator.
Note: To get the absolute value key, you can do one of the following:
a) go to MATH $\square$ NUM and choose option 1 OR
b) press 2nd [CATALOG] and choose the first on the list
(You can find [CATALOG] above the 0 key.)
Graph (Press Zoom 6 for the standard window)


## III. Intersections

Ex. Find the intersection of the following lines $\begin{aligned} & y=3 x-2 \\ & x+2 y=10\end{aligned}$. Here we need to isolate the " $y$ " on the second equation. You can isolate it as $y=-(1 / 2) x+5$ or
$\mathrm{y}=\frac{10-x}{2}$ be sure to use parentheses when entering these expressions into the grapher.
In this case, you would need to enter it as $\mathrm{y}=(10-\mathrm{x}) / 2$
The use of parentheses anytime you have a fraction will keep you out of trouble!

|  |
| :---: |



## To find the intersection:

2nd [CALC] and choose option 5: intersect (Note: The [CALC] key is located above TRACE) Select a first curve and press ENTER; select a second curve and press ENTER; find a guess and press ENTER.


Solution: $x=2$ and $y=4$ or the ordered pair $(2,4)$
Another example: Find the intersection:
$y=-.25 x+3$
$y=x^{2}-5$


Since there are two points of intersection, you will have to find the intersection using the above procedure for each point.
Select a first curve and press ENTER; select a second curve and press ENTER; find a guess and press ENTER. Repeat for the right point.


The calculator will find the first intersection automatically. You need to move the cursor with TRACE $\square$ to find the second point of intersection; repeat the process. The two intersection points (rounded to 3 decimal places) are $(-2.956,3.739)$ and $(2.706,2.323)$.

## IV. Tracing versus finding values

## Trace:

TRACE is useful in graph analyses. When tracing, the x-values are restricted to the interval [Xmin, Xmax]. For values outside of that interval you will have to change the window. The values obtained depend on the window used. You can use the left and right arrows to trace along a curve (or you can enter a value of $x$ by hitting the TRACE key and then a numerical value). If you use the arrows to trace along the curve, the graph will be redrawn as you move beyond the set window and the window will change accordingly Ex. Use your calculator to evaluate $y=x^{3}+3 x^{2}-2 x-2$ at $x=-2.76$ by pressing TRACE and typing a value. You must round your answer to three decimal places.

Graph $y=x^{3}+3 x^{2}-2 x-2$ in the standard window (that is, enter the function under Y1 and press zoom 6), and press TRACE. You will see a value for $x$ and $y$ that depends on where the cursor is placed. Type the number -2.76, press ENTER and you will get $\mathrm{y}=5.348$.


## Value:

Press 2nd [CALC] and choose option 1
Value can be used to evaluate the function at any value within the range [Xmin, Xmax]. It performs similarly to the TRACE key when you enter a value. You can repeat the process by entering other values. If you enter a value that is outside the range, you will get an error message.

Ex. Using your calculator, evaluate $y=x^{3}+3 x^{2}-2 x-2$ at $x=-2.76$ by using the Value Option of the calculator. You must round your answer to three decimal places.

Graph $y=x^{3}+3 x^{2}-2 x-2$ in the standard window. To access the value option, use the CALC function by pressing 2nd TRACEand choosing option number 1 (type 1 or simply press (ENTER)

Type $x=-2.76$, and press ENTER; you will get $\mathrm{y}=5.348$ after rounding.


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## V. Zero

Press 2nd [CALC] and choose option 2
Zero can be used to find the $\mathbf{x}$-value where a function's graph crosses the x -axis (in other words, the $x$-intercept). This is a very useful tool in solving equations. We can solve an equation by moving all the terms to one side of the equation (leaving 0 on the other); then we enter the nonzero side of the equation into the calculator using the $Y$ key. We find the x -intercept(s) of the graph by establishing a left bound and a right bound around the point on the x -axis (using the left and right arrows).

Ex. Find the x-intercepts (or zeros) of $y=x^{3}-3 x^{2}+2$
Graph $y=x^{3}-3 x^{2}+2$ in the window $[-5,5,-5,5]$. That is, a minimum value of -5 for the x and y axes, and a maximum value of 5 .

Press 2nd TRACE, and Press 2 to obtain the zero option (The zero option can also be obtained by using the to select option 2 and pressing [ENTER.)


Since a graph may have more than one x -intercept, you must specify an interval containing the desired x intercept. Let's say that we want to find the x -intercept to the left (see arrow).


When you select the zero option, the question "Left Bound?" appears at the bottom of the screen. Use the calculator arrows to move the blinking cursor to the left of the desired x-intercept, and press ENTER. See the first graph below.

Now the question "Right Bound?" appears at the bottom of the screen; use the $\square$ again to move the blinking cursor to the right of the x -intercept, and press ENTER. See the second graph below.

When the calculator asks "Guess?" just press ENTER to get the x-intercept. See the sequence on the next graphs:





The coordinates of the $x$-intercept appear at the bottom of the last screen.
Let's find the second x-intercept using this "zero" function.


Remember: We need to establish the left and right boundaries, and when the calculator shows "guess" press ENTER to get the x-intercept. See the steps below:


The coordinates of the x-intercept appear at the bottom of the screen.
Now, you try to find the last $x$-intercept using this "zero" function. You should get $\mathrm{x}=2.732, \mathrm{y}=0$.

## VI. Maximum and minimum of graphs

To find Maximum and Minimum points on a graph, use the maximum and minimum options. To find these points, use the CALCULATE feature by pressing 2nd TRACE and choosing option number 3 for minimum, and option number 4 for maximum

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ETLEIILHTE
1:value
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CHLEDUHTE
1:value
2: zero
3:minimum
$4 \mathrm{Bm} \cdot \times 1 \mathrm{~m}$ 네
5: intersect
6: dy dx
7: $5 \mathrm{f}(x) \mathrm{d} x$

Ex. Find the minimum point of. $y=x^{3}-2 x^{2}-x+2$
Graph $y=x^{3}-2 x^{2}-x+2 \quad$ Use ZOOM and select option 4 ("ZDecimal") to have a better viewing window for this example).


Press 2nd TRACE and select option 3
First, we need to specify an interval containing the desired high or low point on the graph by setting the bounds of the function. Since we wish to find the minimum, when the question "Left Bound?" appears at the bottom of the screen, use $\square$ to move the blinking cursor to the left of the relative minimum. Press EENTER. See the first screen on the following page.

When the question "Right Bound?" appears at the bottom of the screen, press $\square$ to move the blinking cursor to the right of the relative minimum. Press ENTER. The arrows at the top of the screen indicate the boundaries between which the calculator will give the relative minimum. (The arrows must point toward each other.)

The question "Guess?" appears at the bottom of the screen; locate the cursor between the established boundaries and press ENTER to display the minimum value. See screens that follow.


The coordinates of the minimum appear at the bottom of the screen.
Ex. Find the maximum point of $\mathrm{y}=\mathrm{x}^{3}-2 \mathrm{x}^{2}-\mathrm{x}+2$.
Graph $y=x^{3}-2 x^{2}-x-2$
Press 2nd TRACE and select option 4, then follow the same steps as before to find a left bound, a right bound and a guess:


You should get the values $\mathrm{x}=-.215$ and $\mathrm{y}=2.113$
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VII Solving Equations Graphically
a) The Intersection Method

Example: Solve $-16 x^{2}+80 x+10=74$ graphically for $x$.
If we apply the Intersection Method, we would enter $Y 1=-16 x^{2}+80 x+10$ and $\mathrm{Y} 2=74$, and find the intersection.

b) The Intercept Method

Example: Solve $-16 x^{2}+80 x+10=74$ graphically for $x$.
If we apply the Intercept Method, we would need to move all terms to one side of the equation; $-16 x^{2}+80 x-64=0$ and find the $x$ intercepts.

| $\begin{array}{\|l\|} \text { Flot Plot Flots } \\ \text { Y1日 } \\ \text { Y1 } \end{array}$ |
| :---: |
| $\mathrm{Y}_{2}=$ |
| Y3 $=$ |
| $\times{ }^{4}=$ |
|  |
| $\mathrm{Y}_{6}=$ |




The $x$ intercepts are 1and 4, as before.

Note: $1 \mathrm{E}-11$ means $1 \times 10^{-11}=.00000000001$
Notice that when using either the Intersection Method or the Intercept Method, we obtain the same answer. The graphs are different, since we are finding the intersection when using one method and the intercept when using the other.

VII Solving inequalities Graphically
a) The intersection Method

Solve $3 \mathrm{x}^{2}+\mathrm{x}<4$ graphically for $x$.
To solve an inequality, first you need to solve the equation, and then interpret the graph

To solve the equation, use the intersection method.



The intersections are the points $(-1.33,4)$ and $(1,4)$. To solve the inequality you need to interpret the graph. The solution of $3 \mathrm{x}^{2}+\mathrm{x}<0$ are all the values of x below the line $\mathrm{y}=4$ and the parabola, or the interval $(-1.33,1)$.
b) The Intercept Method

Solve $3 \mathrm{x}^{2}+\mathrm{x}<4$ graphically for $x$.
To use the intercept method, you need to first solve the equation by moving all the terms to one side of the equation, $3 x^{2}+x-4=0$, and find the $x$-intercepts.




The x intercepts are -1.33 and 1 . To solve the inequality you need to interpret the graph. The solution of $3 x^{2}+x-4<0$ are all the values of $x$ below the $x$-axis, or the interval ( $-1.33,1$ ), the same as the solution above.

