

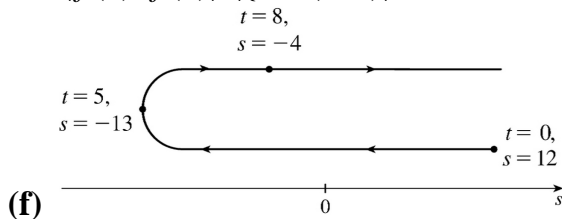
1. (a) $s=f(t)=t^2-10t+12 \Rightarrow v(t)=f'(t)=2t-10$

(b) $v(3)=2(3)-10=-4$ ft / s

(c) The particle is at rest when $v(t)=0 \Leftrightarrow 2t-10=0 \Leftrightarrow t=5$ s.

(d) The particle is moving in the positive direction when $v(t)>0 \Leftrightarrow 2t-10>0 \Leftrightarrow 2t>10 \Leftrightarrow t>5$.

(e) Since the particle is moving in the positive direction and in the negative direction, we need to calculate the distance traveled in the intervals $[0,5]$ and $[5,8]$ separately. $|f(5)-f(0)|=|-13-12|=25$ ft and $|f(8)-f(5)|=|-4-(-13)|=9$ ft. The total distance traveled during the first 8 s is $25+9=34$ ft.



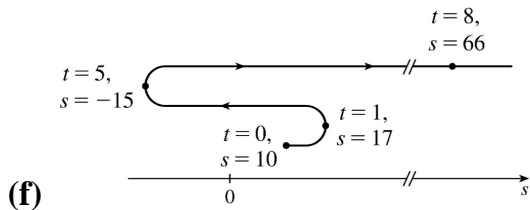
2. (a) $s=f(t)=t^3-9t^2+15t+10 \Rightarrow v(t)=f'(t)=3t^2-18t+15=3(t-1)(t-5)$

(b) $v(3)=3(2)(-2)=-12$ ft / s

(c) $v(t)=0 \Leftrightarrow t=1$ s or 5 s

(d) $v(t)>0 \Leftrightarrow 0 \leq t < 1$ or $t > 5$

(e) $|f(1)-f(0)|=|17-10|=7$, $|f(5)-f(1)|=|-15-17|=32$, and $|f(8)-f(5)|=|66-(-15)|=81$. Total distance $=7+32+81=120$ ft.



10. (a) At maximum height the velocity of the ball is 0 ft / s. $v(t)=s'(t)=80-32t=0 \Leftrightarrow 32t=80 \Leftrightarrow t=\frac{5}{2}$.

So the maximum height is $s\left(\frac{5}{2}\right)=80\left(\frac{5}{2}\right)-16\left(\frac{5}{2}\right)^2=200-100=100$ ft.

(b) $s(t)=80t-16t^2=96 \Leftrightarrow 16t^2-80t+96=0 \Leftrightarrow 16(t^2-5t+6)=0 \Leftrightarrow 16(t-3)(t-2)=0$.

So the ball has a height of 96 ft on the way up at $t=2$ and on the way down at $t=3$. At these times the velocities are $v(2)=80-32(2)=16$ ft / s and $v(3)=80-32(3)=-16$ ft / s, respectively.

21. (a) To find the rate of change of volume with respect to pressure, we first solve for V in terms of P .

$$PV=C \Rightarrow V=\frac{C}{P} \Rightarrow \frac{dV}{dP}=-\frac{C}{P^2}.$$

(b) From the formula for dV/dP in part (a), we see that as P increases, the absolute value of dV/dP decreases. Thus, the volume is decreasing more rapidly at the beginning.

$$(c) \beta = -\frac{1}{V} \frac{dV}{dP} = -\frac{1}{V} \left(-\frac{C}{P^2} \right) = \frac{C}{(PV)P} = \frac{C}{CP} = \frac{1}{P}$$

$$31. (a) A(x) = \frac{p(x)}{x} \Rightarrow A'(x) = \frac{xp'(x) - p(x) \cdot 1}{x^2} = \frac{xp'(x) - p(x)}{x^2}. A'(x) > 0 \Rightarrow A(x) \text{ is increasing; that is,}$$

the average productivity increases as the size of the workforce increases.

$$(b) p'(x) \text{ is greater than the average productivity} \Rightarrow p'(x) > A(x) \Rightarrow p'(x) > \frac{p(x)}{x} \Rightarrow$$

$$xp'(x) > p(x) \Rightarrow xp'(x) - p(x) > 0 \Rightarrow \frac{xp'(x) - p(x)}{x^2} > 0 \Rightarrow A'(x) > 0.$$