

5. (a)  $f(x)$  approaches 2 as  $x$  approaches 1 from the left, so  $\lim_{x \rightarrow 1^-} f(x) = 2$ .

(b)  $f(x)$  approaches 3 as  $x$  approaches 1 from the right, so  $\lim_{x \rightarrow 1^+} f(x) = 3$ .

(c)  $\lim_{x \rightarrow 1} f(x)$  does not exist because the limits in part (a) and part (b) are not equal.

(d)  $f(x)$  approaches 4 as  $x$  approaches 5 from the left and from the right, so  $\lim_{x \rightarrow 5} f(x) = 4$ .

(e)  $f(5)$  is not defined, so it doesn't exist.

7. (a)  $\lim_{t \rightarrow 0^-} g(t) = -1$

(b)  $\lim_{t \rightarrow 0^+} g(t) = -2$

(c)  $\lim_{t \rightarrow 0} g(t)$  does not exist because the limits in part (a) and part (b) are not equal.

(d)  $\lim_{t \rightarrow 2^-} g(t) = 2$

(e)  $\lim_{t \rightarrow 2^+} g(t) = 0$

(f)  $\lim_{t \rightarrow 2} g(t)$  does not exist because the limits in part (d) and part (e) are not equal.

(g)  $g(2) = 1$

(h)  $\lim_{t \rightarrow 4} g(t) = 3$

9. (a)  $\lim_{x \rightarrow -7} f(x) = -\infty$

(b)  $\lim_{x \rightarrow -3} f(x) = \infty$

(c)  $\lim_{x \rightarrow 0} f(x) = \infty$

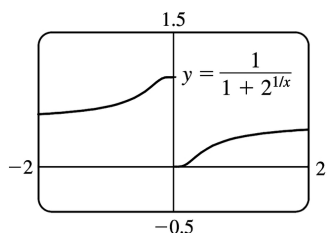
(d)  $\lim_{x \rightarrow 6^-} f(x) = -\infty$

(e)  $\lim_{x \rightarrow 6^+} f(x) = \infty$

(f) The equations of the vertical asymptotes are  $x = -7$ ,  $x = -3$ ,  $x = 0$ , and  $x = 6$ .

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11.



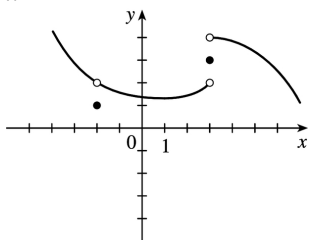
(a)  $\lim_{x \rightarrow 0^-} f(x) = 1$

(b)  $\lim_{x \rightarrow 0^+} f(x) = 0$

(c)  $\lim_{x \rightarrow 0} f(x)$  does not exist because the limits in part (a) and part (b) are not equal.

13.  $\lim_{x \rightarrow 3^+} f(x) = 4$  ,  $\lim_{x \rightarrow 3^-} f(x) = 2$  ,

$\lim_{x \rightarrow -2} f(x) = 2$  ,  $f(3) = 3$  ,  $f(-2) = 1$



17. For  $f(x) = \frac{\sin x}{x + \tan x}$  :

$x$	$f(x)$
$\pm 1$	0.329033
$\pm 0.5$	0.458209
$\pm 0.2$	0.493331
$\pm 0.1$	0.498333
$\pm 0.05$	0.499583
$\pm 0.01$	0.499983

It appears that  $\lim_{x \rightarrow 0} \frac{\sin x}{x + \tan x} = 0.5 = \frac{1}{2}$ .

19. For  $f(x) = \frac{\sqrt{x+4}-2}{x}$  :

$x$	$f(x)$
1	0.236068
0.5	0.242641
0.1	0.248457
0.05	0.249224
0.01	0.249844

$x$	$f(x)$
-1	0.267949
-0.5	0.258343
-0.1	0.251582
-0.05	0.250786
-0.01	0.250156

It appears that  $\lim_{x \rightarrow 0} \frac{\sqrt{x+4}-2}{x} = 0.25 = \frac{1}{4}$ .