

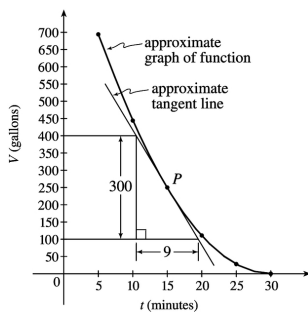
1. (a) Using  $P(15,250)$ , we construct the following table:

$t$	$Q$	slope= $m_{PQ}$
5	(5,694)	$\frac{694-250}{5-15} = -\frac{444}{10} = -44.4$
10	(10,444)	$\frac{444-250}{10-15} = -\frac{194}{5} = -38.8$
20	(20,111)	$\frac{111-250}{20-15} = -\frac{139}{5} = -27.8$
25	(25,28)	$\frac{28-250}{25-15} = -\frac{222}{10} = -22.2$
30	(30,0)	$\frac{0-250}{30-15} = -\frac{250}{15} = -16.\bar{6}$

(b) Using the values of  $t$  that correspond to the points closest to  $P$  ( $t=10$  and  $t=20$ ), we have

$$\frac{-38.8 + (-27.8)}{2} = -33.3$$

(c) From the graph, we can estimate the slope of the tangent line at  $P$  to be  $\frac{-300}{9} = -33.\bar{3}$ .



3. For the curve  $y=x/(1+x)$  and the point  $P\left(1, \frac{1}{2}\right)$ :

(a)

	$x$	$Q$	$m_{PQ}$
(i)	0.5	(0.5,0.333333)	0.333333
(ii)	0.9	(0.9,0.473684)	0.263158
(iii)	0.99	(0.99,0.497487)	0.251256

(iv)	0.999	(0.999,0.499750)	0.250125
(v)	1.1	(1.5,06)	0.2
(vi)	1.5	(1.1,0.523810)	0.238095
(vii)	1.01	(1.01,0.502488)	0.248756
(viii)	1.001	(1.001,0.500250)	0.249875

(b) The slope appears to be  $\frac{1}{4}$ .

(c)  $y - \frac{1}{2} = \frac{1}{4}(x-1)$  or  $y = \frac{1}{4}x + \frac{1}{4}$ .

5. (a)  $y = y(t) = 40t - 16t^2$ . At  $t=2$ ,  $y = 40(2) - 16(2)^2 = 16$ . The average velocity between times 2 and  $2+h$

is  $v_{\text{ave}} = \frac{y(2+h) - y(2)}{(2+h) - 2} = \frac{[40(2+h) - 16(2+h)^2] - 16}{h} = \frac{-24h - 16h^2}{h} = -24 - 16h$ , if  $h \neq 0$ .

(i)  $[2, 2.5] : h=0.5$ ,  $v_{\text{ave}} = -32$  ft / s      (ii)  $[2, 2.1] : h=0.1$ ,  $v_{\text{ave}} = -25.6$  ft / s

(iii)  $[2, 2.05] : h=0.05$ ,  $v_{\text{ave}} = -24.8$  ft / s      (iv)  $[2, 2.01] : h=0.01$ ,  $v_{\text{ave}} = -24.16$  ft / s

(b) The instantaneous velocity when  $t=2$  ( $h$  approaches 0) is  $-24$  ft / s.