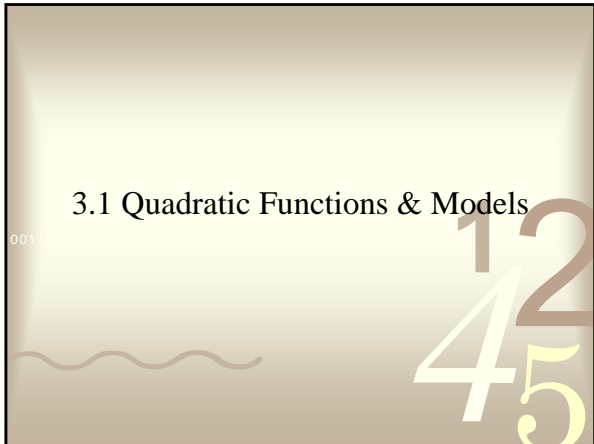


001

### 3.1 Quadratic Functions & Models



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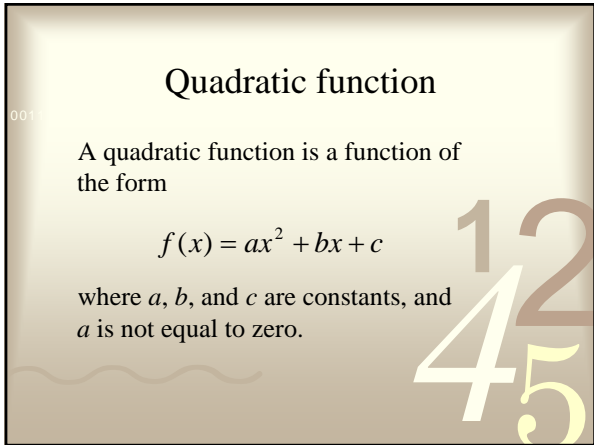
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### Quadratic function

A quadratic function is a function of the form

$$f(x) = ax^2 + bx + c$$

where  $a$ ,  $b$ , and  $c$  are constants, and  $a$  is not equal to zero.



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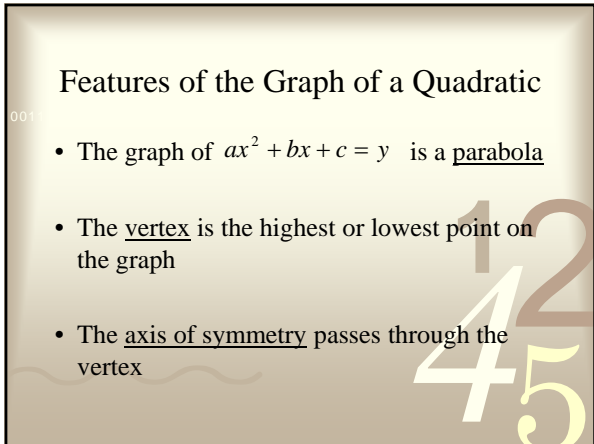
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- 001
- ### Features of the Graph of a Quadratic
- The graph of  $ax^2 + bx + c = y$  is a parabola
  - The vertex is the highest or lowest point on the graph
  - The axis of symmetry passes through the vertex
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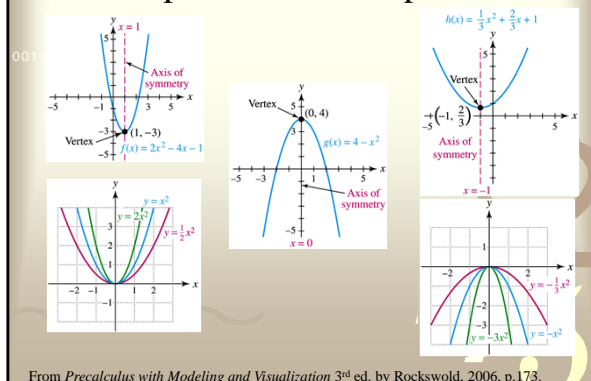
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## Examples of different parabolas




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## Graph of $y = ax^2 + bx + c$

The coefficient of  $x^2$ ,  $a$ , determines the width of the graph.

- If  $|a| < 1$ , the graph is more wide than the graph of  $y = x^2$
- If  $|a| > 1$ , the graph is more narrow than the graph of  $y = x^2$
- If  $a > 0$ , the parabola opens up
- If  $a < 0$ , the parabola opens down

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## Vertex form

The vertex form of a quadratic equation is

$$y = a(x - h)^2 + k$$

where the vertex of the graph is

$$(h, k)$$

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### Example

Sketch the graph of

$$f(x) = (x+1)^2 - 2$$

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### Steps for completing the square

$$y = ax^2 + bx + c$$

1. Make sure the coefficient of  $x^2$  is +1. If it is not, factor  $a$  out of the  $x$  terms only.
2. Square half the coefficient of  $x$  and add to the  $x$  terms and subtract this quantity from  $c$  (remember to multiply by  $a$ , if necessary).
3. Write the result as a perfect square and simplify the constant terms.

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### Examples

- Sketch the graph of  $f(x) = x^2 + 10x + 7$
- Sketch the graph of  $f(x) = 3x^2 + 6x + 2$
- Sketch the graph of  $f(x) = -x^2 + 2x + 1$
- Sketch the graph of  $f(x) = -\frac{1}{2}x^2 + x + 1$

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